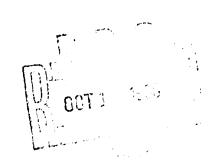
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Technical Memorandum

AN ANALYTICAL METHOD FOR THE DESIGN OF SCORED RUPTURE DIAPHRAGMS FOR USE IN SHOCK AND GUN TUNNELS

by R. W. HENDERSON



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THE JOHNS HOPKINS UNIVERSITY • APPLIED PHYSICS LABORATORY 8621 Georgia Avenue, Silver Spring, Maryland 20910

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LIST OF SYMBOLS

A	cross-sectional area after straining	
Åo	cross-sectional area before straining	
F	force normal to cross-sectional area	
F _P	force normal to pressurized surface	
P	pressure	
S	true stress	
S*	nominal stress	
Su	ultimate stress	
a	radius of rounded edge of opening	
b	radius of opening	
e	base of natural logarithms	
i	length after straining	
i,	length before straining	
m	thinning coefficient (defined in text)	
r ₁	inside radius of curvature of strained diaphragm	
r ₂	radius of curvature at groove bottom	
r ₃	outside radius of curvature of strained diaphragm	
t	thickness of diaphragm material	
α	half angle included by radii at opening	
δ	true strain	
€	nominal strain	
Subscripts		
g	at grooved portion of diaphragm	
ь	at burst condition	

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R.W. Henderson

ABSTRACT

A method of determining burst pressure and petal curvature for a particular diaphragm opening, thickness and score depth is presented which utilizes the plastic stress-strain relationship for the diaphragm material as determined by a conventional tensile test. A comparison of experimental and predicted results is included.

INTRODUCTION

Scored, metal diaphragms are used extensively in shock tubes and gas guns as quick-opening devices. Design of these rupture diaphragms has generally relied on empirical or semi-empirical methods. The practice of scoring so that the diaphragm will open in discrete sections or petals is fairly universal. Two score marks or grooves are usually cut at right angles in one face. Where the depth of the groove is an appreciable portion of the diaphragm thickness, its influence on the burst pressure is evident and must be taken into account. In operation the diaphragm bulges outward into the open area opposite the side being pressurized, the bulge resembling a portion of a sphere. At burst the diaphragm breaks along the score marks into four petals which fold back out of the main flow stream against the sides of the opening.

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Although scoring helps it does not necessarily eliminate undesirable behavior at rupture, such as incomplete opening and breaking off of parts of the diaphragm. In the case of APL's Hypersonic Gun Tunnel, many of the original diaphragms had one or more of their petals knocked off (or bent back across the opening) by the shock waves which are reflected within the gun compression unit. The pieces of flying metal so produced constituted a hazard to the gun's smooth precision bore. The design of these diaphragms was similar to ones successfully used with shock tunnels at the Naval Ordnance Laboratory, White Oak, Maryland. The material used in each instance was 304 stainless steel. Design thicknesses for the series of burst pressures desired for operation at APL were determined from hydraulic burst test of a number of samples of varying thickness. The diaphragms for the higher burst pressures (and in many instances the intermediate burst pressures) in this original series had one or more of their petals knocked off or bent back across the opening when used in the gun. The petals of these diaphragms appeared to have a smaller radius of curvature, that is, to have bulged further into the confine of the opening before rupturing, than those diaphragms which retained their petals (or did not have them bent back across the opening). This led to the speculation that the radius of curvature of the bulge was a factor in petal behavior. With a short radius of curvature the tips of the petals after rupture would project further into the flow stream, whereas with a large radius of curvature they would lie relatively flat against the walls of the opening.

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The bending of the petals laterally by the action of the gas following rupture makes for considerable uncertainty in measuring the amount of curvature at the instant of burst. However, examination of specimens of the design ruptured by hydraulic pressure seemed to confirm a difference in curvature between diaphragms having different design burst pressures. Since the only design variables for a particular burst pressure, material and size of opening are the diaphragm thickness and groove depth, the question is how, if at all, do they affect curvature. The further observation that those diaphragms which lost petals (hence those with apparently smaller radius of curvature) had larger groove to panel thickness ratios indicated the possibility of a relationship of this parameter to curvature.

The following analysis shows that a relationship between thickness ratio and curvature does exist and that burst pressure and petal curvature are functions of the two thicknesses - burst pressure being primarily a function of thickness at the groove bottom, and curvature being a function of diaphragm thickness. The method used is considered to be generally applicable to the design of flat, scored, rupture-diaphragms and may be employed to control petal curvature as well as to determine burst pressure on the basis of diaphragm thickness and score depth.

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ANALYSIS

For the purpose of this analysis a diaphragm of the design shown in Fig. 1a is used. Fressure is applied on the grooved side with the opposite side facing a circular opening having a rounded edge, Fig. 1b. Under the action of pressure, part of the diaphragm bulges outward into the opening, Fig. 2. Treating this part of the diaphragm as a portion of a thin-walled sphere with an inside radius, r_1 , the stress in the wall may be determined by considering an element of the wall with four of its faces under tension of a force, F, Fig. 2. A force, F_p , due to the pressure, P, acts on the inside face of the element over an area $(\Delta t)^2$ and

$$F_{p} = P(\Delta \ell)^{2} = P r_{1} \Delta \alpha \Delta \ell.$$
 (1)

This force is balanced by the four tensile forces acting on the lateral faces of the element. From a vector diagram, Fig. 2, of the forces in one plane,

$$F\Delta\alpha = 1/2 F_{p}. \tag{2}$$

Substituting for F_p

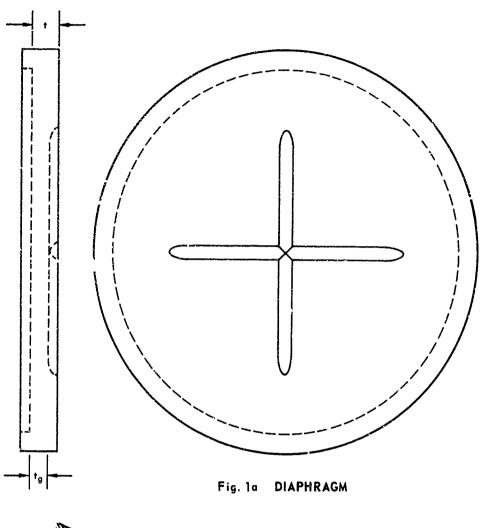
$$F = 1/2 P r_1 \Delta \ell. \tag{3}$$

The area of each lateral face is

$$A = t/m \Delta \ell \tag{4}$$

where t is the initial thickness and m is a coefficient to correct for the thinning caused by stretching the material. Combining terms, the following expression for the stress, S, in the strained diaphragm wall is obtained:

$$S = \frac{F}{A} = \frac{\frac{1}{2} Pr_1 \Delta \ell}{\frac{E}{m} \Delta \ell} = \frac{Pr_1}{2 \frac{E}{m}}.$$
 (5)



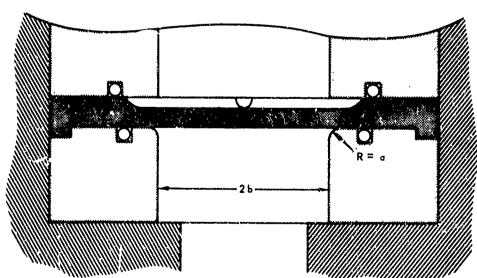
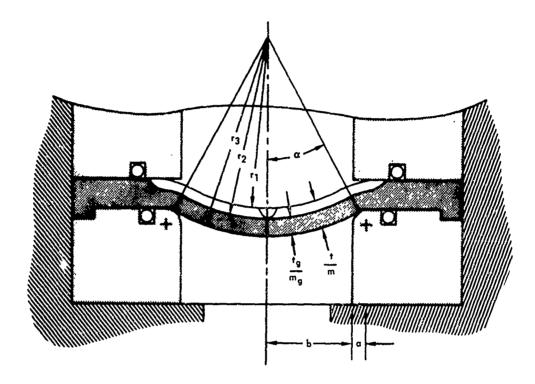


Fig. 16 DIAPHRAGM AND HOLDER

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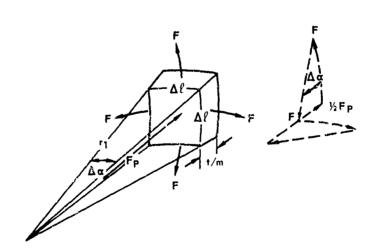


Fig. 2 STRAINED DIAPHRAGM

Since the same tensile force acts in the grooved portion of the diaphragm as in the wall, the stress in this part, S_g , is to the stress in the wall as the inverse ratio of their respective cross-sectional areas; that is,

$$\frac{S}{S} = \frac{\frac{t}{m} \Delta \ell}{m} = \frac{\frac{t}{m}}{m}$$

$$S = \frac{t}{m} \Delta \ell = \frac{t}{m}$$

$$\frac{S}{S} \Delta \ell = \frac{t}{m}$$

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where t is the initial thickness at the groove and $\ensuremath{\mathtt{m}}$ is its thinning coefficient.

The term stress, as used here thus far, may be referred to as the true stress as opposed to the nominal stress, the value conventionally determined in a tensile test of the material. The true stress and strain are defined 3 as:

True stress =
$$\frac{F}{A}$$
 = S (7)

where F is the load and A is the actual cross-section after straining.

True strain =
$$\ln \frac{\ell}{\ell_0} = \hat{0}$$
 (8)

where ℓ is the length after straining and ℓ_0 is the original length. The nominal stress and strain are defined as:

Nominal stress =
$$\frac{F}{A_0}$$
 = S' (9)

where F is the load and A_{o} is the original cross-sectional area; and

Nominal strain =
$$\frac{\ell - \ell_0}{\ell_0} = \epsilon$$
 (10)

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where ℓ_0 and ℓ are the original and strained length respectively. From their definitions, then, the true stress is to the nominal stress as the original cross-sectional area is to the area after straining; that is,

$$\frac{S}{S'} = \frac{A_{O}}{A} \tag{11}$$

and the true and nominal strains have the following relationship to one another:

$$e^{\delta} = \varepsilon + 1 = \frac{\iota}{\iota_0}. \tag{12}$$

Most of the diaphragm deformation occurs above the yield condition for the material, see Fig. 3. The change in volume of a material during the first stage of plastic deformation (i.e., prior to necking) is negligible. Hence, assuming constant volume, the original volume, $V_0 = A_0 \dot{t}_0$, equals the volume after straining, $V = A \dot{t}_0$, so that

$$\frac{A_0}{A} = \frac{\iota}{\iota_0} \tag{13}$$

In the case of the element of diaphragm wall previously considered, the cross-sectional area for the elemental width $\Delta \ell$ is t $\Delta \ell$ before straining and t/m $\Delta \ell$ afterwards so that

$$\frac{A_0}{A} = \frac{t \Delta \ell}{t \Delta \ell} = m. \tag{14}$$

The thinning coefficient, therefore, corresponds to the ratio of the initial to strained cross-sectional areas, and the following relationships between the thinning coefficient and true and nominal stress and strain are obtained:

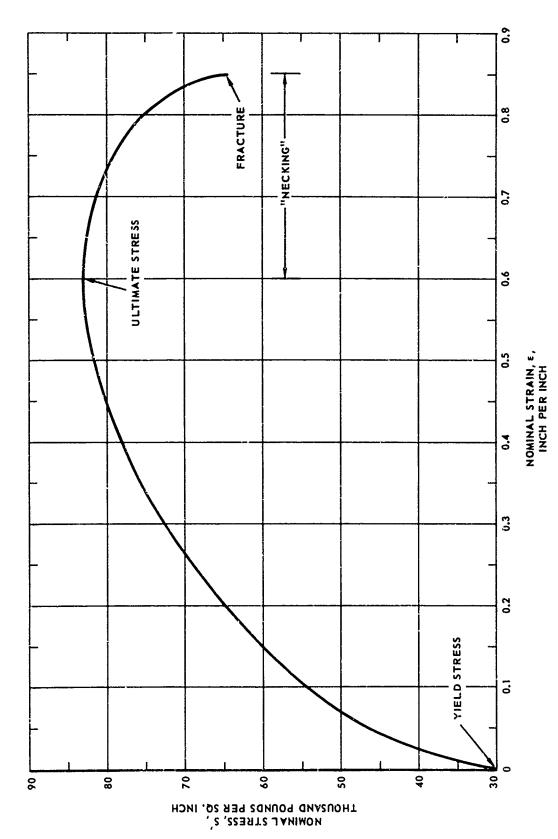


Fig. 3 STRESS-STRAIN DIAGRAM, 30% STAINLESS STEEL PLASTIC REGION

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$$\frac{S}{S'} = e^{\delta} = \varepsilon + 1 = m. \tag{15}$$

Equation (5) may now be written in terms of the nominal stress as

$$S' = \frac{\Pr_{1*}}{2!} \tag{16}$$

Equation (6) may be written as

$$\frac{S'}{S'} = \frac{t}{t_g} \tag{17}$$

since the above relationships of stress, strain and thinning coefficient would also hold for the material in the grooved part of the diaphragm.

The nominal stress in the grooved portion of the diaphragm is greater than that in the rest of the wall by a factor of $\frac{t}{t_g}$ (t_g being less than t), and the diaphragm will rupture at the groove when S'g reaches the ultimate stress for the material, S'u. The nominal stress in the wall at the burst condition, then, is proportional to the thickness ratio; that is,

$$(S')_b = \frac{r_g}{t} \quad S'_u. \tag{18}$$

Since stress and strain are functions of one another as determinable from a tensile test of the material, the strain and, thereby, the thinning coefficient are also functions of the thickness ratio at the burst condition.

^{*} This is the familiar expression for the stress in a thin-walled sphere where the stress is assumed to be evenly distributed across the wall thickness.

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Referring to Fig. 2, the length at any cross section of the part of the diaphragm in the opening is 2(a+b) before straining and $2(a\alpha+r_3\alpha)$ afterwards, so the nominal strain at any point in the deformed portion may be represented as

$$\varepsilon = \frac{\ell - \ell_0}{\ell_0} = \frac{2(a + r_3) \alpha - 2(a + b)}{2(a + b)} = \frac{(a + r_3) \alpha}{a + b} - 1.$$
 (19)

Noting in Fig. 2 that

$$\frac{a+b}{a+r_3} = \sin \alpha \tag{20}$$

the strain may be written in terms of α or r_3 . The strain and, thereby, the stress and thinning coefficients are all functions of r_3 for an opening of radius b with rounded edge of radius a. Thus r_3 for a given opening is also a function of the thickness ratio at the burst condition. Equation (5) may be written in terms of r_3 , since $r_1 + \frac{t}{m} = r_3$, as

$$S = \frac{P}{2} \left(\frac{mr_3}{t} - 1 \right) = mS^{\dagger}. \tag{21}$$

Therefore, for a particular opening and diaphragm material, the burst pressure may be determined for a given set of values of t and t since S', m and r₃ at the burst condition are all functions of $\frac{t_g}{t}$.

A typical nominal stress-strain diagram for 304 stainless steel is shown in Fig. 3. The relationship of α to the nominal strain and the thinning coefficient is presented in Fig. 4. Figure 5 shows the true

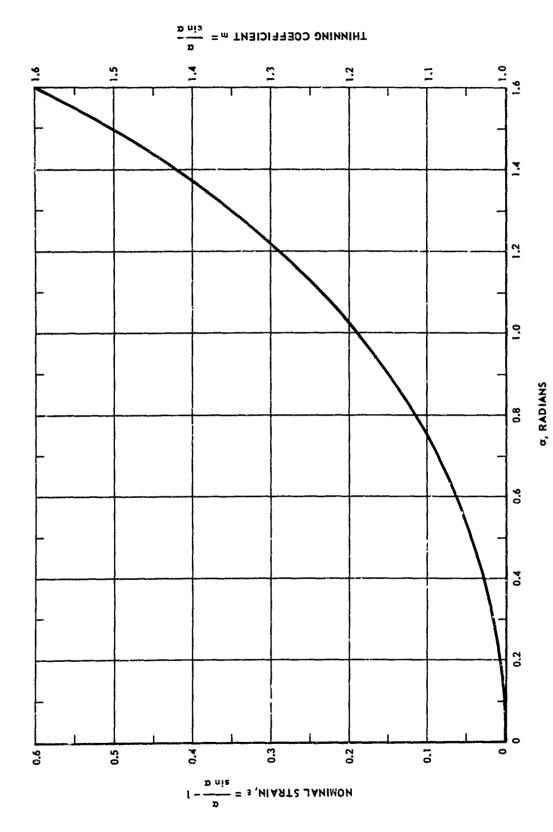
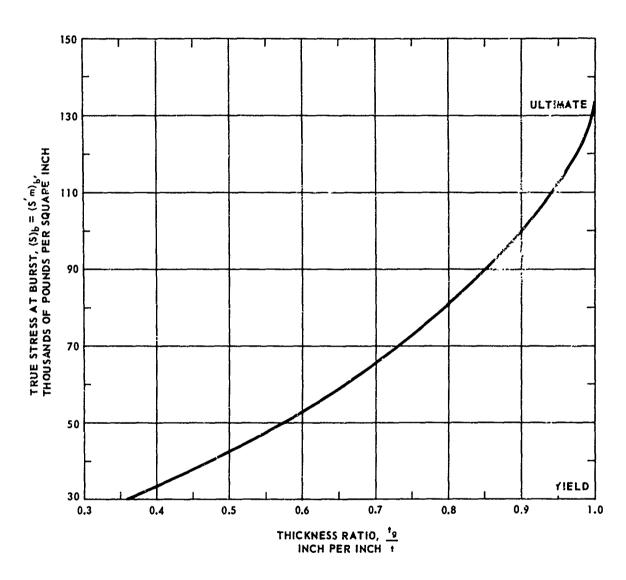


Fig. 4 THINMING COEFFICIENT AND NOMINAL STRAIN VERSUS INCLUDED HALF ANGLE



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Fig. 5 TRUE STRESS AT BURST VERSUS THICKNESS RATIO

stress in the diaphragm wall at the burst condition as a function of the thickness ratio; and Fig. 6 shows the relationship of thickness ratio to α at the burst condition. These curves are generally applicable to the design of 304 stainless steel diaphragms of the type shown in Fig. 1 and may be used for any given size of opening to determine the thicknesses required for a given burst pressure. For an opening of radius b having a rounded edge of radius a, α may be determined with relationship to α from Equation (20) and referring to Figs. 4 and 6 a plot made of α vs α vs α remarks and the relationship of S to α respectively. From this and the relationship of S to α resolves as has been done in Fig. 7 for the gun tunnel opening.

RESULTS AND CONCLUSIONS

Average values of diaphragm burst pressure and thickness based on data from forty-seven gun tunnel tests are shown in Fig. 7 with their thickness ratios for comparison with the analytically predicted values. These experimental values are for the 304 stainless steel diaphragms initially used in the APL Hypersonic Gun Tunnel. The majority of tests were made at the 5500 and 7500 psi levels. The variations in nominal burst pressure for the diaphragms tested were on the order of \pm 500 psi and the variation in thickness on the order of \pm .002 inches. Petalling was satisfactory for those diaphragms having nominal burst pressure of 3500 and 5500 psi, erratic at the 7500 psi level, and generally poor for those above. This fall-off in petal behavior with increasing pressure (and

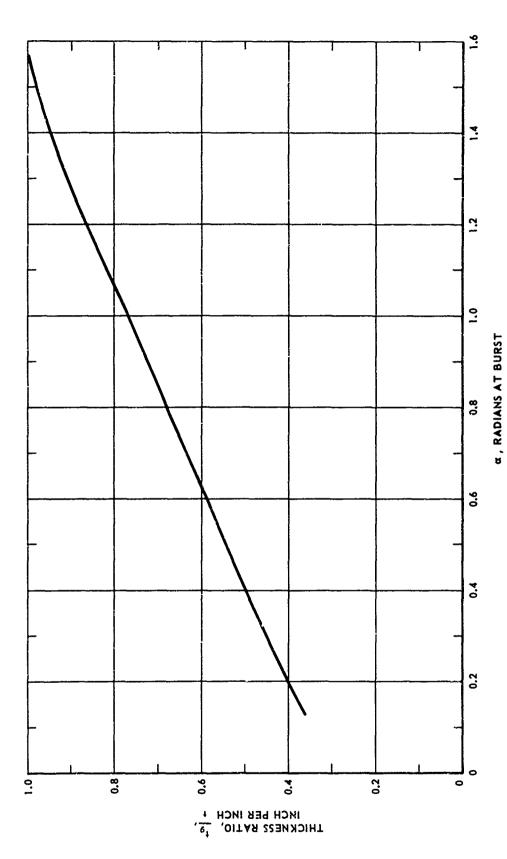


Fig. 6 THICKNESS RATIO VERSUS INCLUDED HALF ANGLE AT BURST

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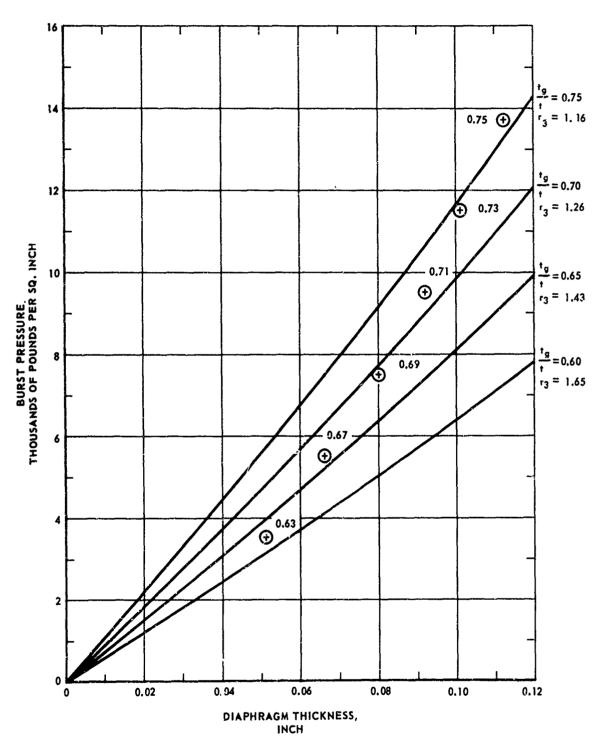


Fig. 7 BURST PRESSURE VERSUS THICKNESS FOR VARIOUS THICKNESS RATIOS

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thickness) is accompanied by a decrease in the radius of diaphragm curvature which may be seen in Fig. 7 where the outside radii corresponding to the thickness ratio for the curves are also given. Figure 8 uses the radii determined from the thickness ratios for the 3500 and 13,500 psi diaphragms to compare the amount of petal projection into the opening.

Where reflected shock waves are present, the amount of diaphragm petal curvature can be a factor in pecal damage. The extent to which pressure and thickness are involved in petalling is not immediately evident from this study; however, an optimum value, or range of values, of thickness ratio apparently does exist for satisfactory petalling. This value is on the order of 0.65 for the diaphragms studied. Further investigation of this and the other factors could prove to be very useful in eliminating petalling problems.

The good correlation of experimental and analytical results indicates that the method of analysis may be generally useful in designing rupture diaphragms. It should be noted that the edge of the diaphragm is held at its periphery so that lateral slippage is essentially eliminated. The degree to which burst pressure may be fixed is limited in practice by the uniformity of material and thickness that can be attained in fabrication. The deviation in burst pressure for the diaphragms tested is less than would be predicted analytically for the observed thickness tolerance and is as small as can reasonably be expected in this case. The tolerances in any given situation will depend on the opening size, material and pressure involved.

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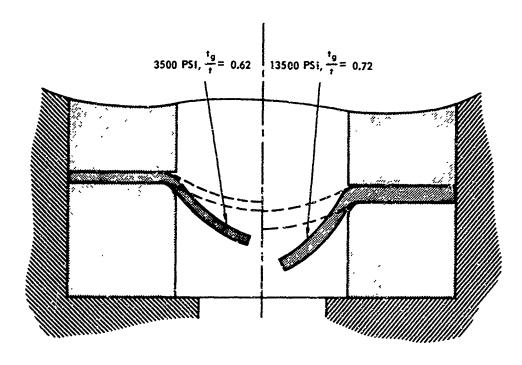


Fig. 8 COMPARISON OF PETAL PROJECTION

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